

GEOG 362 Introduction to Remote Sensing and image processing
Problem Set #1, Fall 2011

1. Go to the following URL to answer the next couple questions:

<http://www.lon-capa.org/~mmp/applist/Spectrum/s.htm>

- a.) **How does wavelength vary with frequency?** A longer wave length will have a lower frequency due to fewer waves passing a point over the same amount of time of a shorter wavelength which would have a higher frequency. This relationship is often times referred to as being an inverse one where one value increases the other decreases.
- b.) **What wavelength ranges correspond to the sizes of atomic nuclei?** Atomic nuclei are found in wavelengths from $6.711 \times 10^{-13} \text{m}$ (6.7nm) up to $5.577 \times 10^{-12} \text{m}$ (0.005nm) according to the slider bar provided.
- c.) Put the following forms of light – ultraviolet, infrared, gamma rays, visible, radio, X-rays **In order of increasing frequency** (lowest frequency first):
Radio, infrared, visible, ultraviolet, X-rays, Gamma rays
Put them in order of increasing wavelength (shortest wavelength first).
Gamma rays, X-rays, ultraviolet, visible, infrared, radio
Put them in order of increasing energy (lowest energy first).
Radio, infrared, visible, ultraviolet, X-rays, Gamma rays

2. Review the content on the following website and answer the following questions:

<http://www.astronomynotes.com/light/s3.htm#A1.1>

Convert the following wavelengths to frequency assuming an electromagnetic wave traveling through free space:

- a.) $0.450 \text{ um} = .45 \times 10^{-6} \text{m} = 4.5 \times 10^{-7} \text{m}$ $f = c/\lambda = 2.99 \times 10^8 \text{ m/s} / 4.5 \times 10^{-7} \text{m}$ = 6.44e14 hertz
- b.) $2.5 \text{ um} = 2.5 \times 10^{-6} \text{m}$ $f = c/\lambda = 2.99 \times 10^8 \text{ m/s} / 2.5 \times 10^{-6} \text{m}$ = 1.19e14 hertz
- c.) $1 \text{ cm} = .01 \text{ m}$ $f = c/\lambda = 2.99 \times 10^8 \text{ m/s} / .01 \text{ m}$ = 2.99e10 hertz

2. Besides each number of wavelengths listed below, please indicate the category (e.g. Infrared or Microwave) which each wavelength belongs to.

- | | |
|---|--|
| $6.5 \times 10^{-7} \text{ m}$ <u>Visible Orange/Red</u> | $0.42 \text{ um} = 4.2 \times 10^{-7} \text{m}$ <u>Visible Blue/Purple</u> |
| $1 \times 10^{-13} \text{ m}$ <u>Gamma Rays</u> | 2 m <u>Radio Waves</u> |
| $1.2 \times 10^{-5} \text{ m}$ <u>Infrared/Heat Radiation</u> | $3.765 \text{ cm} = 0.03765 \text{m}$ <u>Microwaves/Radar</u> |

3. Supposed there are two individual photons, one's wavelength is $0.75 \mu\text{m}$, and the other one's is $3.0 \mu\text{m}$. Please compare the amount of energy two photons have and answer which one has higher energy. (Show your steps)

We know the Frequency and wavelength relation: $f = c/\lambda$

This shows an inverse relationship between Frequency and wavelength.

We also know the following: Energy of a photon: $E = hf$, where h is a constant of nature called "Planck's constant" = $6.63 \times 10^{-34} \text{ J}\cdot\text{sec}$.

The amount of energy a photon has or produces is directly proportional to its frequency. A higher frequency (short wave length) has a higher energy level than a photon experiencing a low frequency (long wave length). This means as Frequency increases, so does the energy of a photon

With that said, a wave length of $0.75 \mu\text{m}$ is shorter than a wave length of $3.0 \mu\text{m}$. This means the shorter wavelength ($0.75 \mu\text{m}$) has the higher frequency and therefore the higher energy as well.

To Prove this here are the calculation of each photons energy

Photon 1: $f = c/\lambda = 2.99e8 \text{ m/s} / 7.5e-7\text{m} = 3.98e14 \text{ hertz}$

$$E = hf = 6.63 \times 10^{-34} \text{ J}\cdot\text{sec} * 3.98e14 \text{ hertz}$$

$$E = 2.63e-19 \text{ J}$$

Photon 2: $f = c/\lambda = 2.99e8 \text{ m/s} / 3.0e-6\text{m} = 9.96e13 \text{ hertz}$

$$E = hf = 6.63 \times 10^{-34} \text{ J}\cdot\text{sec} * 9.96e13 \text{ hertz}$$

$$E = 6.60e-20 \text{ J}$$

$$E = 2.63e-19 \text{ J} > E = 6.60e-20 \text{ J}$$

E Photon 1 > E Photon 2